

### Lossless Join Example discussed in class

Let  $R = ABCDE$ ,  $R_1 = AD$ ,  $R_2 = AB$ ,  $R_3 = BE$ ,  $R_4 = CDE$ , and  $R_5 = AE$ . Let the functional dependencies be:  $A \rightarrow C$ ,  $B \rightarrow C$ ,  $C \rightarrow D$ ,  $DE \rightarrow C$ ,  $CE \rightarrow A$

Apply algorithm 7.2 from class handout to test if the decomposition of  $R$  into  $\{R_1, \dots, R_5\}$  is a lossless join decomposition.

The initial table looks as follows:

	A	B	C	D	E
R1(AD)	<b>a1</b>	b12	b13	<b>a4</b>	b15
R2(AB)	<b>a1</b>	<b>a2</b>	b23	b24	b25
R3(BE)	b31	<b>a2</b>	b33	b34	<b>a5</b>
R4(CDE)	b41	b42	<b>a3</b>	<b>a4</b>	<b>a5</b>
R5(AE)	<b>a1</b>	b52	b53	b54	<b>a5</b>

Apply FD  $A \rightarrow C$  to the initial table to modify the violating dependencies. Rows 1, 2, 5 will need to change the values for the RHS attribute C – equate b13, b23, b53 to b13 (you might very well have picked b23 or b53 to equate all three). We won't change the rows 3 & 4 yet because their symbols b31, b41 are different from a1.

A	B	C	D	E
<b>a1</b>	b12	<del>b13</del> <b>b13</b>	a4	b15
<b>a1</b>	a2	<del>b23</del> <b>b13</b>	b24	b25
b31	a2	b33	b34	a5
b41	b42	a3	a4	a5
<b>a1</b>	b52	<del>b53</del> <b>b13</b>	b54	a5

Apply  $B \rightarrow C$  next to equate b33 with b13

A	B	C	D	E
a1	b12	<del>b13</del> <b>b13</b>	a4	b15
a1	<b>a2</b>	<del>b23</del> <b>b13</b>	b24	b25
b31	<b>a2</b>	<del>b33</del> <b>b13</b>	b34	a5
b41	b42	a3	a4	a5
a1	b52	<del>b53</del> <b>b13</b>	b54	a5

Next, use  $C \rightarrow D$  to equate a4, b24, b34, and b54

A	B	C	D	E
a1	b12	<del>b13</del> <b>b13</b>	<b>a4</b>	b15
a1	a2	<del>b23</del> <b>b13</b>	<del>b24</del> <b>a4</b>	b25
b31	a2	<del>b33</del> <b>b13</b>	<del>b34</del> <b>a4</b>	a5
b41	b42	a3	a4	a5
a1	b52	<del>b53</del> <b>b13</b>	<del>b54</del> <b>a4</b>	a5

DE → C helps us to equate b13 (all occurrences) with a3. The following table shows the corresponding changes.

A	B	C	D	E
a1	b12	<del>b13</del> <b>b13</b> a3	a4	b15
a1	a2	<del>b23</del> <b>b13</b> a3	<del>b24</del> a4	b25
b31	a2	<del>b33</del> <b>b13</b> a3	<del>b34</del> a4	<b>a5</b>
b41	b42	<b>a3</b>	<b>a4</b>	<b>a5</b>
a1	b52	<del>b53</del> <b>b13</b> a3	<del>b54</del> a4	<b>a5</b>

Apply CE → A to the table above to equate b31, b41, and a1.

A	B	C	D	E
a1	b12	<del>b13</del> <b>b13</b> a3	a4	b15
a1	a2	<del>b23</del> <b>b13</b> a3	<del>b24</del> a4	b25
<del>b31</del> <b>a1</b>	<b>a2</b>	<del>b33</del> <b>b13</b> a3	<del>b34</del> a4	<b>a5</b>
<del>b41</del> <b>a1</b>	b42	<b>a3</b>	a4	<b>a5</b>
<b>a1</b>	b52	<del>b53</del> <b>b13</b> a3	<del>b54</del> a4	<b>a5</b>

The middle row in the table above is all a's, and the decomposition has a lossless join.

What happens if we apply FDs in a different order?

Try any FD with the same symbols (a or b) on the LHS attribute in at least two rows. We have two choices: A → B or B → C. We tried A → B in the previous test. Try B → C here.

A	B	C	D	E
<b>a1</b>	b12	b13	<b>a4</b>	b15
<b>a1</b>	<b>a2</b>	<del>b23</del> b23	b24	b25
b31	<b>a2</b>	<del>b33</del> b23	b34	<b>a5</b>
b41	b42	<b>a3</b>	<b>a4</b>	<b>a5</b>
<b>a1</b>	b52	b53	b54	<b>a5</b>

Apply A → C after that to get the following table. Notice I chose b23 to equate b13, b23, and b53.

A	B	C	D	E
<b>a1</b>	b12	<del>b13</del> b23	<b>a4</b>	b15
<b>a1</b>	<b>a2</b>	<del>b23</del> b23	b24	b25
b31	<b>a2</b>	<del>b33</del> b23	b34	<b>a5</b>
b41	b42	<b>a3</b>	<b>a4</b>	<b>a5</b>
<b>a1</b>	b52	<del>b53</del> b23	b54	<b>a5</b>

The table shown above is the similar to the one we got before after applying A → C and B → C to the initial table. To the current table we apply C → D as before because we have the same symbol b23 in rows 1, 2, 3, and 5.